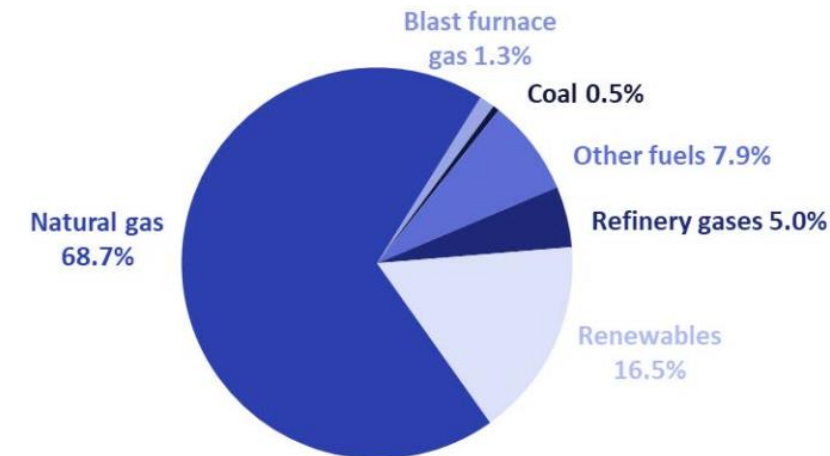
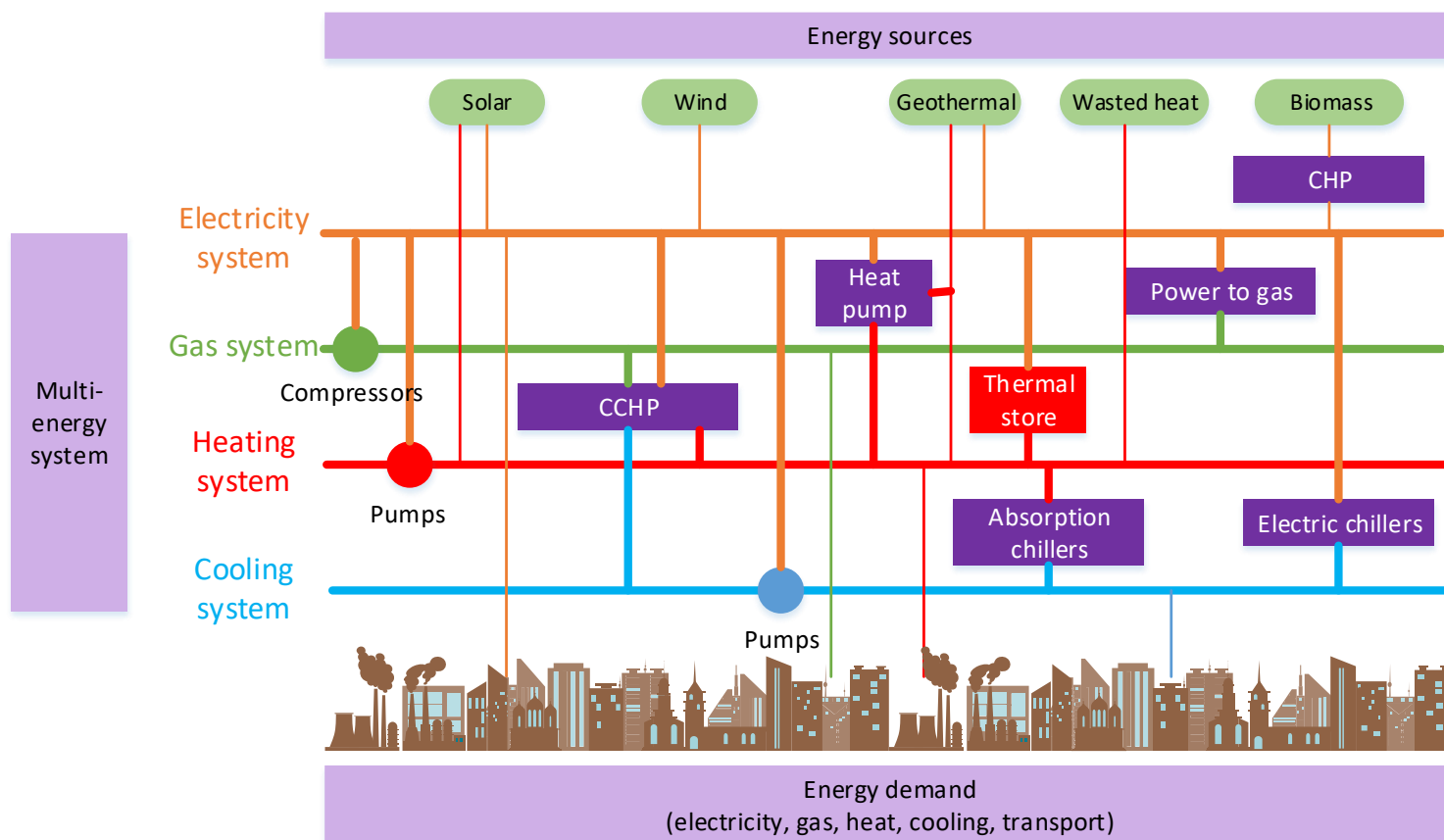


Operational Reliability Evaluation of Distributed Multi-Energy Systems Considering Optimal Control of Energy Storages

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Introduction



- **68.7%** of the fuel used in CHP schemes in 2017 was natural gas in UK [1].
- In China, the heat demand of nearly 9×10^9 m² area is supplied by centralized heating supply, 51% of which is met by CHP

Multiple energy sources, transmission and distribution systems and energy demands are organized for production, delivery and consumption, especially **electricity**, **gas** and **heat** in demand side.

Introduction

Reliability issues

2017.08

Taiwan,
China



- Human error in Datan gas fired power plant
- Interruption of gas supply
- 4 GW electricity shortage

2020.12

Shanxi,
China



- Freeze of the coal handling belt of the heating and power plant
- interruption of the heat supply for the urban district of 11 km² for three days

2021.02

Texas,
US



- Freeze of the gas well valves
- 20 GW load shedding, interruption of over 4.8 million users

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Our work

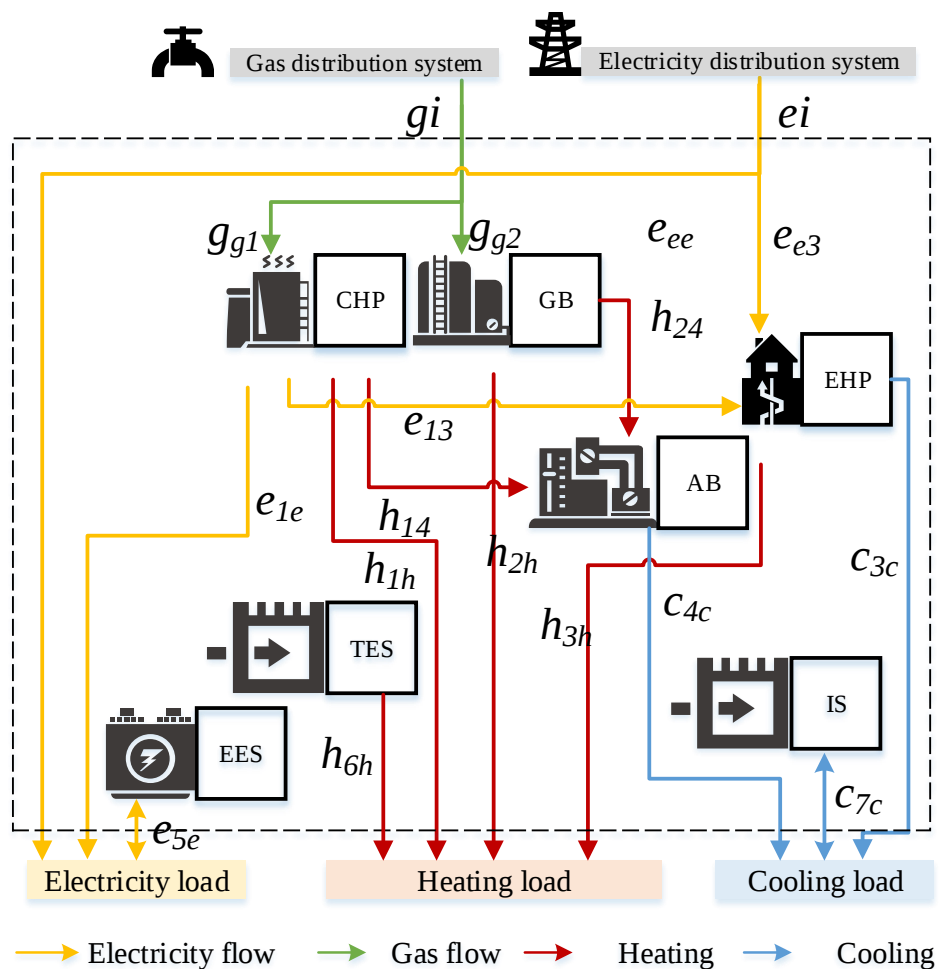
Long-term



Short-term

- Time-varying load curve
- Time-varying state probability
- Optimal control actions

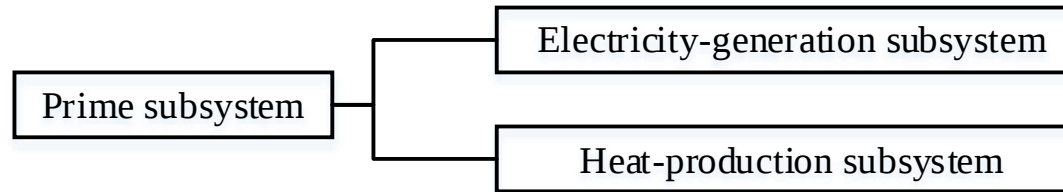
Structure of the studied DMES



- Combined heat and power plant (CHP)
- gas boiler (GB)
- electric heat pump (EHP)
- absorption chiller (AB)
- electric energy storage (EES)
- thermal energy storage (TES)
- ice storage (IS)

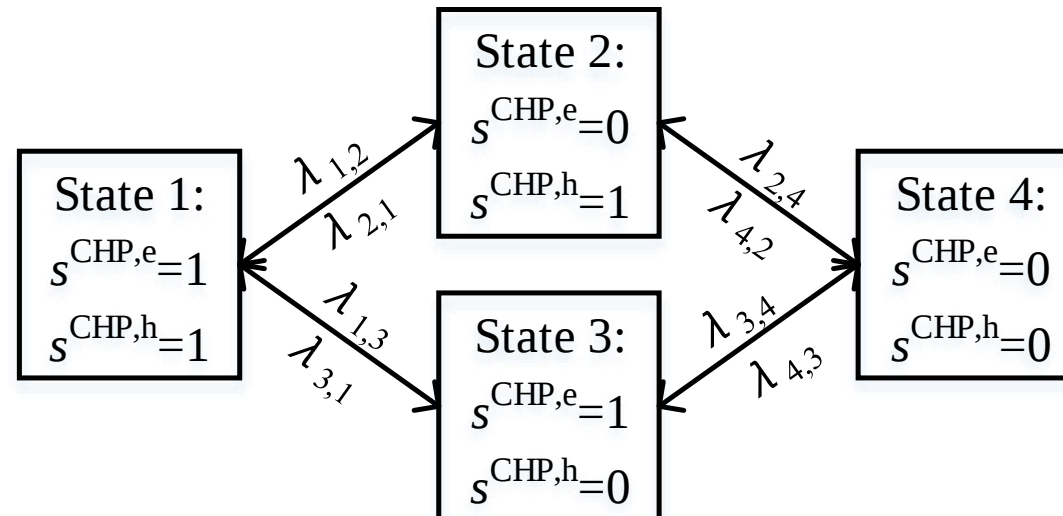
Operational reliability of the components

Structure



$$s^{CHP,h} = s^p s^h, s^{CHP,e} = s^p s^e$$

State transition



• State transition rate

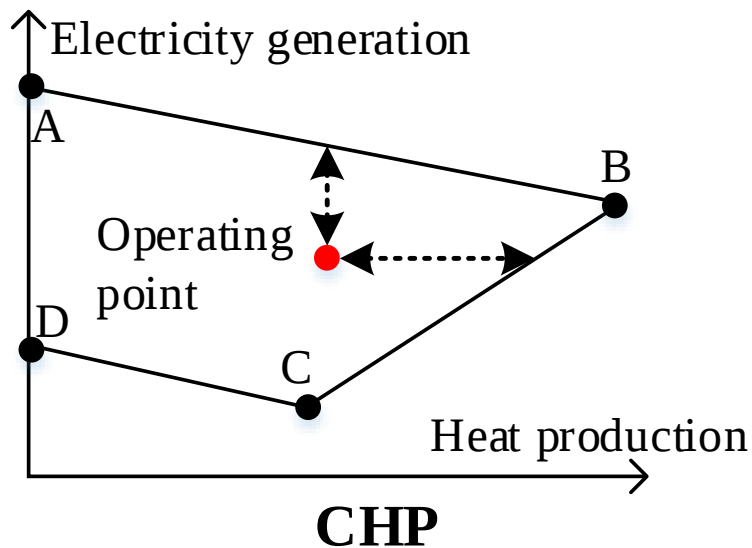
$$\lambda_{1,2} = \lambda^e, \lambda_{2,1} = \mu^e \quad \lambda_{1,3} = \lambda^h, \lambda_{3,1} = \mu^h \quad \lambda_{2,4} = \lambda^h + \lambda^p, \lambda_{3,4} = \lambda^e + \lambda^p$$

$$\lambda_{4,2} = \left(\Pr\{s^p = 1, s^e = 0, s^h = 0\} \mu^h + \Pr\{s^p = 0, s^e = 0, s^h = 1\} \mu^p \right) / \left(\Pr\{s^p = 1, s^e = 0, s^h = 0\} + \Pr\{s^p = 0, s^e = 0, s^h = 1\} \right)$$

$$\lambda_{4,3} = \left(\Pr\{s^p = 1, s^e = 0, s^h = 0\} \mu^e + \Pr\{s^p = 0, s^e = 1, s^h = 0\} \mu^p \right) / \left(\Pr\{s^p = 1, s^e = 0, s^h = 0\} + \Pr\{s^p = 0, s^e = 1, s^h = 0\} \right)$$

Operational reliability of the components

Operating constraints



In the
normal
state

$$h_{1h} + h_{14} \geq 0$$

$$e_{13} + e_{1e} - E_A - (E_A - E_B) / (H_A - H_B)(h_{1h} + h_{14}) \leq 0$$

$$e_{13} + e_{1e} - E_B - (E_B - E_C) / (H_B - H_C)(h_{1h} + h_{14} - H_B) \geq 0$$

$$e_{13} + e_{1e} - E_D - (E_C - E_D) / (H_C - H_D)(h_{1h} + h_{14}) \geq 0$$

In the
failure
state

$$s^{CHP,h} = 1, s^{CHP,e} = 0$$

$$e_{13} + e_{1e} = 0$$

$$\min\{H_A, H_B, H_C, H_D\} \leq h_{1h} + h_{14} \leq \max\{H_A, H_B, H_C, H_D\}$$

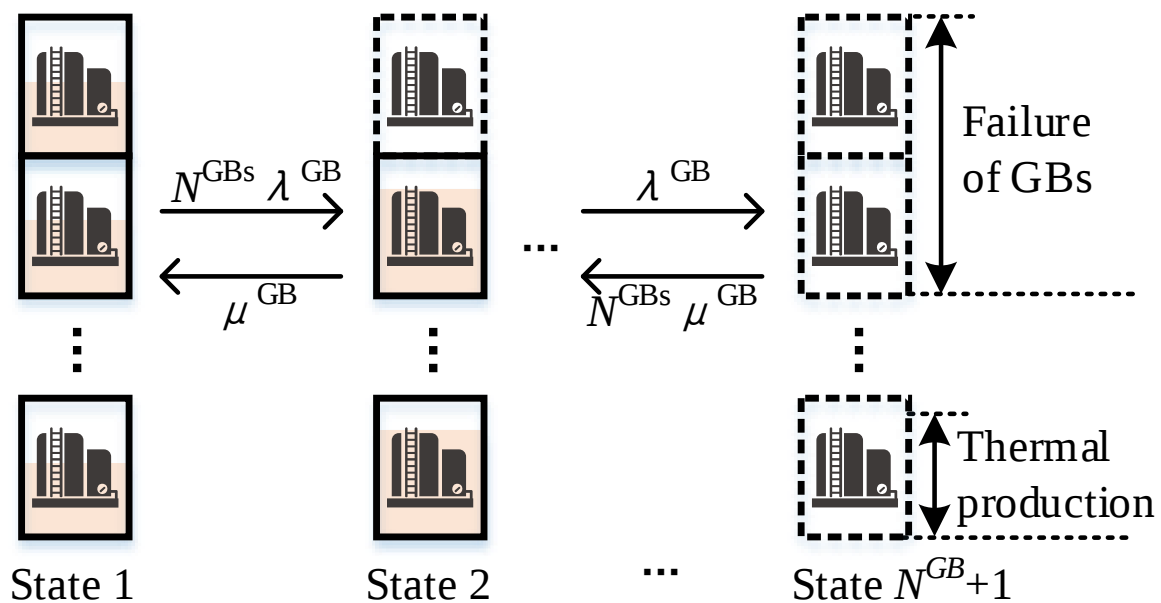
$$s^{CHP,h} = 0, s^{CHP,e} = 1$$

$$h_{1h} + h_{14} = 0$$

$$\min\{E_A, E_B, E_C, E_D\} \leq e_{13} + e_{1e} \leq \max\{E_A, E_B, E_C, E_D\}$$

Operational reliability of the components

Gas boilers



- Operating constraints

$$0 \leq h_{24} + h_{2h} \leq \frac{N^{GBs} + 1 - s^{GBs}}{N^{GBs}} ho_2^+$$

- State transition rates

$$\lambda_{s^{GBs}, s^{GBs}+1}^{GBs} = (N^{GBs} + 1 - s^{GBs}) \lambda^{GB}$$

$$\lambda_{s^{GB}, +1s^{GB}}^{GB} = s^{GBs} \mu^{GB}$$

Optimal control during the component failure

Objective function

$$\text{Min } C = \sum_{k \in K} \rho_k^g (g_{g1,k} + g_{g2,k}) + \rho_k^e (e_{ee,k} + e_{e3,k}) + \sum_{l \in \{el, th, cl\}} CDF^l(T_{s_k}) lc_k^l$$

Control variables

$$g_{g1}, g_{g2}, e_{ee}, e_{e3}, e_{1e}, e_{13}, h_{1h}, h_{14}, h_{2h}, h_{24}, c_{3c}, h_{3h}, c_{4c}, e_{5e}, h_{6h}, c_{7c}, es_5, es_6, es_7$$

Constraints

- CHP constraints
- Energy conversion constraints:

$$\mathbf{H} \begin{bmatrix} ei & gi & \mathbf{u} \end{bmatrix}^T =$$

$$\begin{bmatrix} d^{el} - lc^{el} & d^{th} - lc^{th} & d^{cl} - lc^{cl} & \mathbf{0} \end{bmatrix}^T$$

- Operating constraints of GBs, EHPs, and ABs

$$0 \leq c_{4c} \leq co_4^+(N^{ABs} + 1 - s^{ABs}) / N^{ABs}$$

$$0 \leq h_{3h} \leq \gamma ho_3^+(N^{EHPs} + 1 - s^{EHPs}) / N^{EHPs}$$

$$0 \leq c_{3c} \leq (1 - \gamma) co_3^+(N^{EHPs} + 1 - s^{EHPs}) / N^{EHPs}$$

$$\mathbf{u}_k \geq 0$$

- Operating constraints for energy storages

$$|e_{5e}| \leq eo_5^+(N^{EESs} + 1 - s^{EESs}) / N^{EESs}$$

$$|e_{5e}| \leq eo_5^+(N^{EESs} + 1 - s^{EESs}) / N^{EESs}$$

$$|c_{7c}| \leq co_7^+(N^{ISs} + 1 - s^{ISs}) / N^{ISs}$$

$$es_{5,k} = es_{5,k-1} + e_{5e} \Delta t$$

$$es_{6,k} = es_{6,k-1} + h_{6h} \Delta t$$

$$es_{7,k} = es_{7,k-1} + c_{7c} \Delta t$$

$$0 \leq es_{5,k} \leq es_5^+(N^{EESs} + 1 - s^{EESs}) / N^{EESs}$$

$$0 \leq es_{6,k} \leq es_6^+(N^{TESs} + 1 - s^{TESs}) / N^{TESs}$$

$$0 \leq es_{7,k} \leq es_7^+(N^{ISs} + 1 - s^{ISs}) / N^{ISs}$$

Reliability evaluation procedures

- Reliability indices

$$EDNS^l(k) = \sum_{i=1}^{NS} lc_k^l / NS$$

$$LOLP^l(k) = \sum_{i=1}^{NS} flag(lc_k^l) / NS$$

- Convergence criterion

$$\sqrt{Var(EDNS^l(k))} / EDNS^l(k) \leq \xi$$

Step 1

- input data. Including the physical characteristics of the DMES, the reliability parameters, and the load profile.
- Set the duration of the operation horizon.

Step 2

- simulate the state sequence of each component using TSMCS.
- Combine them into the system state sequence.

Step 3

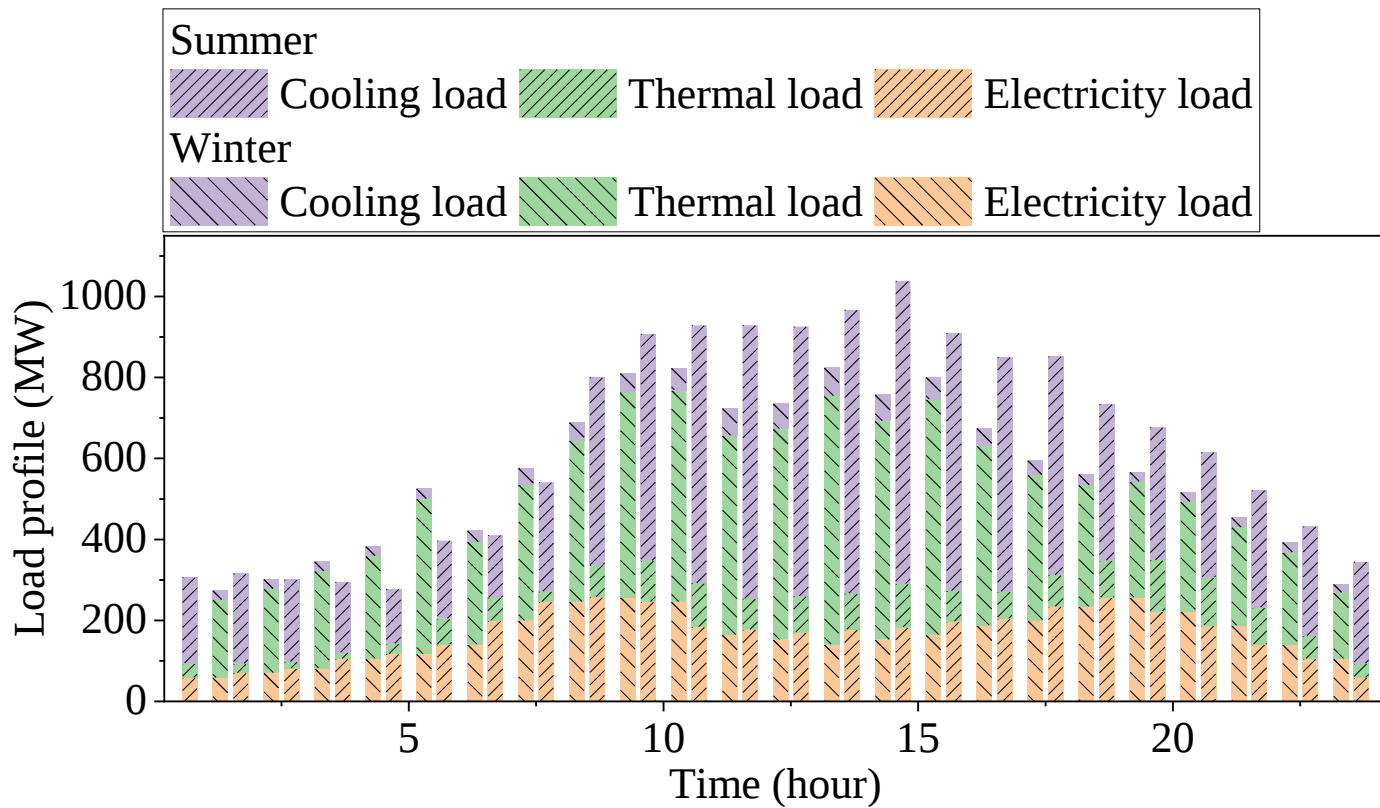
- formulate the optimal control problem over the operational horizon.
- Solve the linear optimal control problem using the Gurobi solver, and obtain the load curtailment for each energy.

Step 4

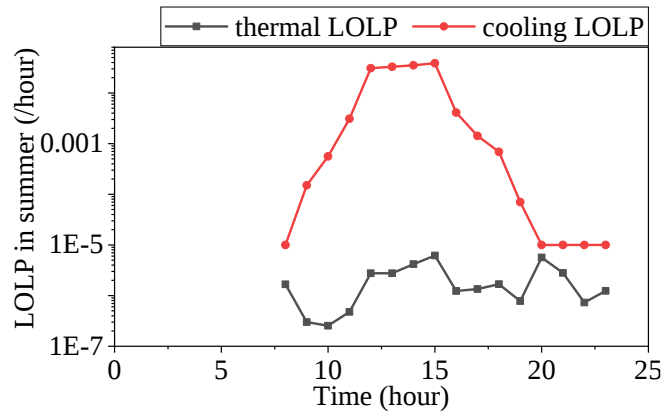
- Calculate the reliability indices.
- Check for convergence. If satisfies, then output the operational reliability indices. Otherwise, repeat from step 2 for the next simulation.

Case studies

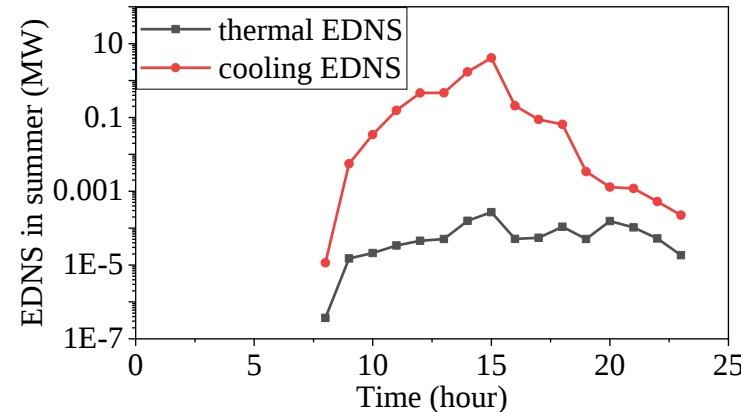
load profiles



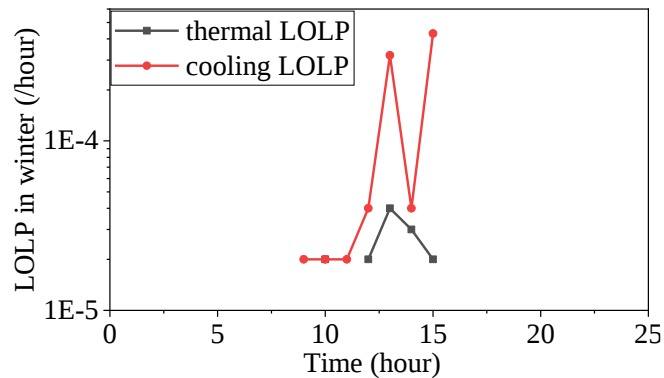
Case studies



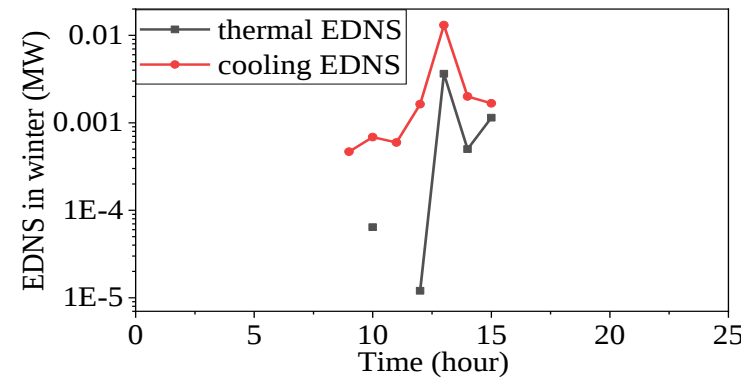
LOLP in summer



EDNS in summer



LOLP in winter



EDNS in winter

- In both seasons, the EDNS and LOLP of electricity remains 0.
- Other two energies remain zero until 8 : 00. The EDNS and LOLP emerge during 8:00-23:00.
- In summer, the LOLP and EDNS of cooling are higher than those in winter.
- the LOLP and EDNS of thermal load are lower than those in winter.

Thank you

